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# Separation of vibration fringe data from rotating object fringes using pulsed ESPI

Carlos Pérez López<sup>a</sup>, Fernando Mendoza Santoyo<sup>a,\*</sup>,  
Ramón Rodríguez Vera<sup>a</sup>, Marcelo Funes-Gallanzi<sup>b</sup>

<sup>a</sup>Centro de Investigaciones en Óptica, A.C., Loma del Bosque 115, León, Gto. 37150, Mexico

<sup>b</sup>Instituto Nacional de Astrofísica Óptica y Electrónica, Luis Enrique Erro 1, Tonantzintla, Puebla, Pue.  
72840, Mexico

## Abstract

In industrial and other types of non-controlled environments, an unbalanced rotating object may present characteristic out-of-plane vibration amplitude at a specific frequency. For this type of cases and as a first step towards a complete evaluation, it is only desired to visualize the effect of the vibration on the rotating object, or vice versa, for instance to achieve object balancing. Real time optical non-intrusive measurement techniques such as pulsed electronic speckle pattern interferometry (ESPI), are well suited to study this rotating-vibrating object. The advantage offered by ESPI is that real-time fringe data is qualitatively analyzed while being observed on a TV monitor. The present paper proposes a qualitative method, based on pulsed ESPI, to separate rotation fringes from fringes solely related to vibration. The method relies on a high precision scheme that synchronizes and fixes an object point during rotation, without the use of an optomechanical object derotator. © 2002 Published by Elsevier Science Ltd.

*Keywords:* Electronic speckle pattern interferometry; Twin pulsed laser; Vibration and rotation fringes

## 1. Introduction

Speckle decorrelation on a moving object is a major problem in a dynamic electronic speckle pattern interferometry (ESPI) system. In particular for a rotating object, speckle decorrelation is present if the object angular displacement is larger than the average speckle diameter on the CCD sensor. Some solutions to this

\*Corresponding author. Fax: + +52-4-717-50-00.

E-mail address: fmendoza@foton.cio.mx (F.M. Santoyo).

1 problem have been proposed [1–4], in particular the use of two laser pulses to freeze  
 2 the object movement between two different object positions. Fringes from a rotating  
 3 object relate mainly to (a) deformations solely due to its rotation, for instance  
 4 stresses due to the centrifugal force and out-of-plane vibrations, among others, and  
 5 (b) the object angular displacement. Several research works report on methods to  
 6 eliminate the rotation fringes by using an optomechanical derotator and on-axis  
 7 illumination setups [5,6]. The use of the former devices requires a great deal of  
 8 manipulation and hence is time consuming. Here, an alternative method to analyze  
 9 object displacements in dynamic conditions, particularly while rotating, is presented.

10 The method is based on a high precision scheme that synchronizes [7] and fixes an  
 11 object point during rotation. The interferometer is set to be sensitive to out-of-plane  
 12 rigid body displacements by employing two laser pulses that illuminate the object  
 13 along the rotation axis. For the analysis, the inherent rotation fringes may be seen as  
 14 carrier fringes. A small object angular displacement between the firing of two laser  
 15 pulses converts into a slope of the out-of-plane displacement, which is added to the  
 16 carrier fringes, i.e., fringes due to out-of-plane displacement are modulated by the  
 17 carrier fringes. As is customary, in addition to pulsed ESPI, the speckled interference  
 18 patterns obtained from each of the pulses are added in a single frame of the CCD  
 19 camera. Addition fringes are noisy and thus difficult to see on the monitor. However,  
 20 in order to recover addition fringes at video rate, an analogue electronic filter [8,9] is  
 21 employed. The method shows that any object unbalance may be detected by simply  
 22 observing the changes in angular direction and frequency of the carrier fringes. With  
 23 this method, there is no need to perform a phase calculation to obtain a displacement  
 24 measurement, since the latter is achieved by time tracking the object vibration with  
 25 respect to a rotating axis.

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## 28 2. Principle of the method

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30 The mathematical model for addition fringe formation in pulsed ESPI will be  
 31 briefly described, since it may be found elsewhere, viz., [2]. Assume an unknown  
 32 object displacement while it rotates, and that two laser pulses are fired within a CCD  
 33 frame. All variables have  $(x, y)$  dependence, where coordinate axes  $(x, y)$  are fixed at  
 34 the center of the CCD camera faceplate. The intensity on the CCD faceplate for  
 35 pulse 1 is

$$36 I_1 = I_o + I_r + 2\sqrt{I_o I_r} \cos(\phi) \quad (1)$$

37 and for pulse 2,

$$38 I_2 = I_o + I_r + 2\sqrt{I_o I_r} \cos(\phi + \Delta\psi + \rho), \quad (2)$$

39 where as usual,  $I_o$  and  $I_r$  denote the object and reference beam intensity, respectively.  
 40  $\phi$  is the random speckle phase,  $\Delta\psi$  is the phase term due to object deformation alone,  
 41  $\Delta\psi = 4\pi\delta z(t)/\lambda$ , and  $\rho$  is the phase term associated to object rotation. Notice that  
 42 Eq. (1) assumes that the object is rotating, but its motion is frozen during the 15 ns  
 43 laser pulse width such that the equation does not contain  $\Delta\psi + \rho$ . Eq. (2) does  
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1 contain these phase terms since the second pulse is fired some microseconds after the  
 2 first pulse, i.e., the object rotated and displaced. The addition of both pulsed speckle  
 3 interferograms is done within a CCD frame, giving

$$5 \quad I_t = 2(I_o + I_r) + 4\sqrt{I_o I_r} \cos\left(\phi + \frac{\Delta\psi}{2} + \frac{\rho}{2}\right) \cos\left(\frac{\Delta\psi}{2} + \frac{\rho}{2}\right). \quad (3)$$

7 In practice, the object beam lies in the  $x'z'$  plane, coordinate axes set on the object, in  
 8 such a way that the phase variable  $\rho$  can be uniquely expressed in terms of the  $y'$   
 9 object coordinate as

$$11 \quad \rho = \frac{2\pi}{\lambda}(y' \sin \alpha)\theta. \quad (4)$$

13 The angle  $\theta$  is chosen such that  $\rho$  represents, through Eq. (4), the object rotation  
 14 contribution to the interferometer out-of-plane sensitivity vector, i.e.,  $\theta$  is small.  
 15 Besides,  $\theta$  allows for the formation of vertical carrier fringes. The angle  $\alpha$  is the object  
 16 rotation angle between pulses 1 and 2, with elapsed time  $t$ . This angular displacement  
 17 renders rotation fringes under the following condition:

$$19 \quad t < \frac{\lambda F}{2\pi \omega R}, \quad (5)$$

21 where  $\lambda$  is the wavelength of the laser light used,  $F$  is the  $f$ -number of the ESPI  
 22 system imaging lens,  $\omega$  is the object rotation frequency, and  $R$  its radii. The idea in  
 23 using the fringes obtained in rotation as carrier fringes, to be later distinguished from  
 24 out-of-plane displacement fringes, allows the displacement data  $\delta z(t)$  to be analyzed  
 25 as a change in fringe angular direction and frequency. To avoid the speckle  
 26 decorrelation effects imposed by Eq. (5), the interferogram in Eq. (3) should be taken  
 27 within that time limit. Experimentally and in present day applications, only shorter  
 28 time separations, than those expressed in Eq. (5), are of interest.

29 The addition interferogram, Eq. (3), is electronically filtered so that it may be  
 30 represented by a cosinusoidal fringe pattern,  $I_f$ . In fact the filter is designed to  
 31 eliminate the first cosine term, a high frequency term [10], in the equation. Thus the  
 32 argument of the cosine function that remains is the sum of  $\Delta\psi$  plus  $\rho$ . The time lapse  
 33 between the two pulses is of the order of  $1 \mu\text{s}$ , allowing us to introduce in  $\Delta\psi$  the  
 34 slope of the object displacement as a function  $\delta z(t)/\delta t$ . This slope is evaluated at the  
 35 same object angular position, e.g., each time the object completes one revolution.  
 36 The final filtered speckle interferogram  $I_f$  depends on the slope of the temporal  
 37 object displacement:

$$37 \quad I_f = K \cos(b\delta z(t)/\delta t + \rho/2), \quad (6)$$

39 where  $K$  is a filter constant that depends mainly on the filter gain, and  $b = 2\pi\delta t/\lambda$ . It  
 40 can be seen from Eq. (6) that the out-of-plane object displacement and rotation  
 41 influence the frequency and angular direction of the resulting fringes. The out-of-  
 42 plane object displacement is directly related to the object out-of-plane tilt over the  
 43  $x'z'$  and  $y'z'$  planes.

45 As mentioned, it is necessary to acquire the twin pulsed addition speckle  
 46 interferograms at the same object angular position. The synchronization method

1 used in order to study the same object position is depicted in Fig. 1, whose top shows  
 2 the CCD camera even and odd fields that would contain interferometric data. There  
 3 are three conditions that the synchronization has to meet in order to have laser  
 4 pulses falling inside CCD camera fields. (A) The CCD camera used has a NTSC  
 5 system at 30 frames per second, so the laser has to deliver pulses at 60 Hz, even when  
 6 the object rotating position is not the expected, a point widely explained in Ref. [7].  
 7 (B) In order to have interferometric data in the CCD camera fields, the object  
 8 rotation frequency  $\omega$  has to be equal to that of the external signal synthesizer. It  
 9 should be noticed that some of the CCD camera fields have no information. (C) The  
 10 twin laser pulses should be fired within to the initial and final CCD camera field, i.e.,  
 11 the laser should be synchronized with the camera. Finally, once the above conditions  
 12 have been met, a pulse delay unit is used to visually freeze the object rotating motion,  
 13 as seen on the TV monitor of the ESPI system, so that every image is captured at the  
 14 same object position. A diagram block of the above procedure is shown at the  
 15 bottom of Fig. 1. The synchronization operation accuracy was visually checked, a  
 16 feature that is easily seen on the TV monitor by freezing the object rotation on the  
 17 screen.

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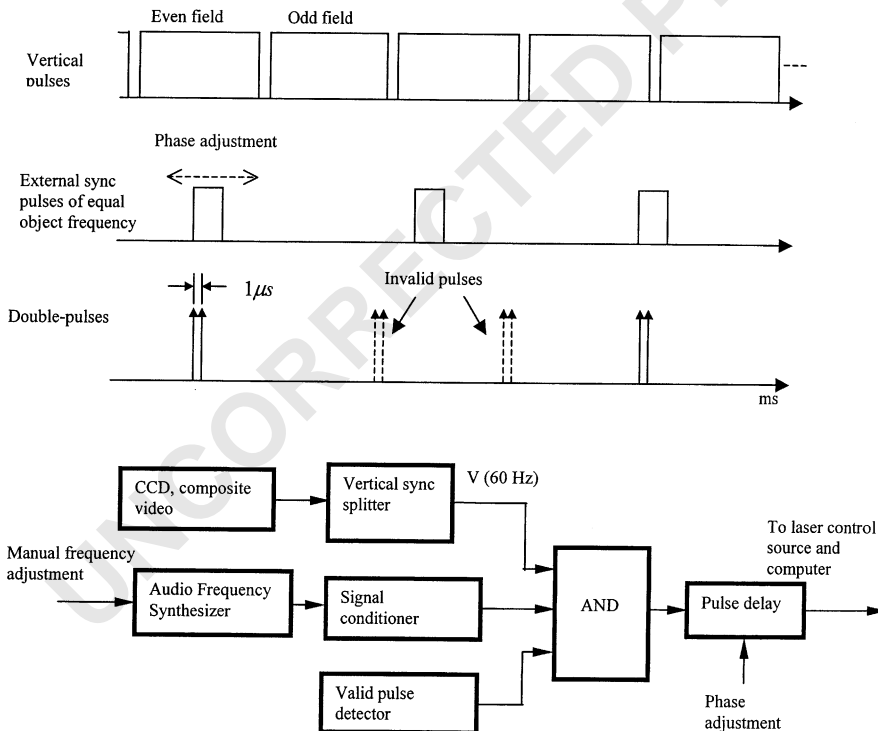


Fig. 1. Schematic diagram for the synchronization method.

### 1 3. Experiments and results

3 A typical out-of-plane ESPI arrangement is show in Fig. 2. Light from a Nd:YAG  
 5 twin pulsed laser is divided in two at the beam splitter BS, to be used as the reference  
 7 and object beams. The illuminated rotating object is imaged onto a CCD camera by  
 9 a zoom lens. Previously, an object beam calibration is needed to reduce the rotation  
 11 fringes to only three vertical fringes. The object under study is a rotating fan, whose  
 13 blades rotate at  $\omega = 1200$  rpm. The blades are considered to be plane and  
 perpendicular to the line of observation. The laser was operated at approximately  
 20 mJ per pulse, with  $\lambda = 532$  nm, 15 ns laser pulse width, and a pulse rate of 60 Hz.  
 The CCD camera used had a faceplate with  $640 \times 480$  pixels. A frame grabber inside  
 a Pentium III PC is instructed to capture the speckle interferograms corresponding  
 to Eqs. (1) and (2), for out-line processing.

A computer fringe simulation is shown in Fig. 3, where Eq. (6) was used to  
 perform the calculations. Fig. 3a shows fringes due to rotation only,  $\rho/2$ . Fig. 3b has  
 an object out-of-plane tilt along the  $x'z'$  plane. Notice that this tilt increases the  
 fringe frequency only. In Fig. 3c, an out-of-plane combination on both  $x'z'$  and  $y'z'$   
 planes has been added, a feature that shows a change in the angular direction of the  
 fringes. For Fig. 3d, an out-of-plane object tilt was introduced along the  $y'z'$  plane,

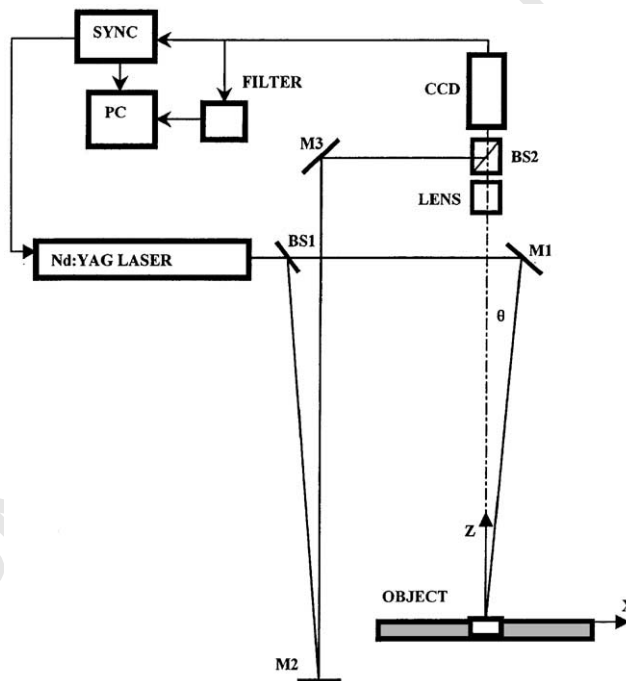


Fig. 2. Out-of-plane twin pulsed ESPI set-up as used for the vibrating analysis of rotating objects. BS1–2 are beam splitters, and M1–3 mirrors.

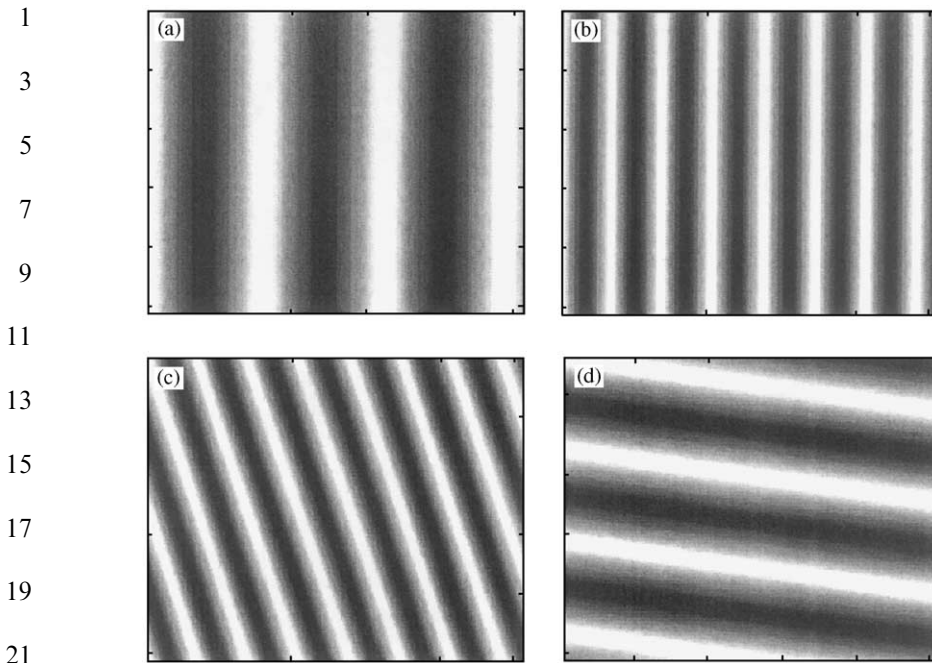


Fig. 3. Computer simulated fringes with an out-of-plane tilt introduced in b-d.

together with a subtraction of the term for object rotation. These figures were calculated with the purpose of emulating the experimental results to be shown next. For the case of a harmonic vibration of the rotating object, fringe patterns will be cyclic, meaning that if Fig. 3b represents a starting point, this pattern will repeat after some time. The time chosen for the computed images was 10 s.

The synchronization scheme explained before, allows the image acquisition with a predefined time pulse separation  $t = 900$  ns, such that each object blade is seen exactly at the same position when each of the two pulses are fired. The synchronization yields a typical addition interferogram shown in Fig. 4a. The successive images are taken from exactly the same, apparently static, object position. The electronic filtering was made with a RC high pass filter, matched to a diode envelope detector to adapt TV positive voltages. Fig. 4b shows the filter action when detecting carrier fringes with the object rotating at 1200 rpm. Even with the characteristic additive noise, three vertical carrier fringes due to rotation can be observed on the TV monitor. In Fig. 4c, an object tilt along the  $y'$  axis, as described by Eq. (6), produces an increment in the vertical fringe frequency. Figs. 4d and e show a tilt combination on both  $x'$  and  $y'$  axes, affecting the angular direction and frequency of the fringes. In Fig. 4f, there is an object tilt contribution in  $x'$ , however the  $y'$  tilt is in the opposite sense to the one for the carrier fringes, showing a near-horizontal fringe pattern. The images in Fig. 4 were taken in a lapse time of 10 s.

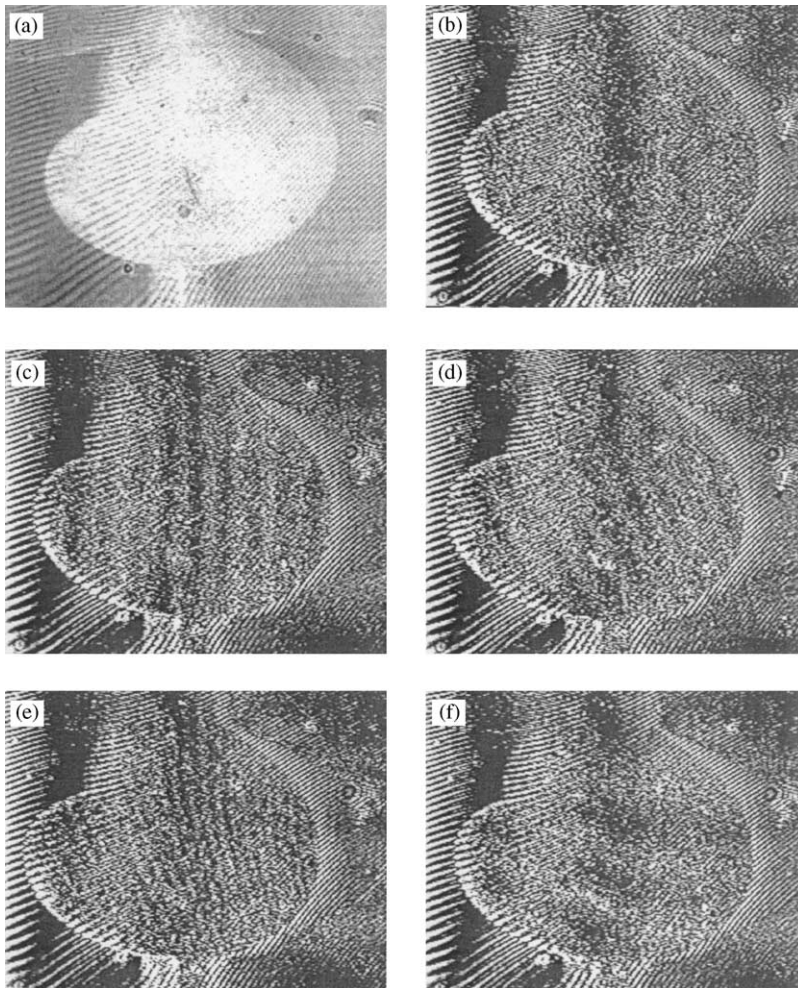


Fig. 4. A frozen blade of the rotating fan is shown. Out-of-plane tilt fringes may be observed in c-f. Compare these images to the ones in Fig. 3.

#### 4. Conclusions

The addition ESPI method presented shows that it is possible to qualitatively study out-of-plane vibrations at video rate for rotating objects. The method is capable of separating vibration fringes from the inherent rotation fringes when a controlled synchronization and illumination arrangement are used. The advantage of directly watching on a TV monitor the addition interferogram, electronically filtered, allows reducing the time lapse between two images to obtain slopes of instant object displacement. Further considerations will have to take into account the blade shape, and simultaneously illuminated object points in order to obtain 3D

1 displacement vectors. Absolute measurement of displacements requires the inclusion  
2 of a  $z$  position controller. The method is suited to study out-of-plane vibrations in  
3 noisy environments. Finally, future research along the lines of this paper will be  
4 carried out shortly in order to quantify the data obtained with the aforementioned  
5 method, and to evaluate the system uncertainty with respect to the object angular  
6 position accuracy which was beyond the scope of the research results presented here.

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